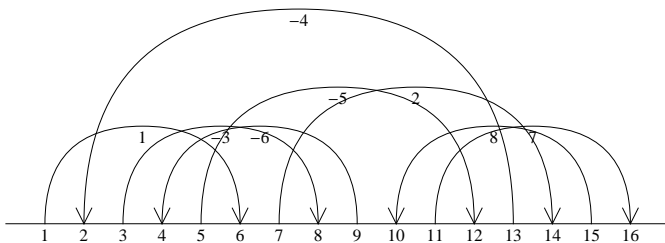


Pensieve Header: Testing row sums.

```
<< KnotTheory`
GD[K_] := GD @@ (
  PD[K] /. X[i_, j_, k_, l_] => If[PositiveQ[X[i, j, k, l]],
    Ar[l, i, +1], Ar[j, i, -1]
  ]
)
```

Loading KnotTheory` version of August 22, 2010, 13:36:57.55.
Read more at <http://katlas.org/wiki/KnotTheory>.

```
Draw[expr_] := expr /. gd_GD => Draw[gd];
Draw[gd_GD] := Module[
  {n = Length[gd], h, k = 0},
  Graphics[
    Line[{{0, 0}, {2 n + 1, 0}}],
    Table[Text[i, {i, -0.3}], {i, 2 n}],
    (List@@gd) /. {
      Ar[i_, j_, s_] => {
        h = Abs[i - j] / 2;
        BezierCurve[
          {i, 0}, {i, h}, {(i + j) / 2, h}, {j, h}, {j, 0}
        ], SplineDegree -> 2],
      Text[s * (++k), {(i + j) / 2, h - 0.3}],
      Line[{{j - 0.2, 0.4}, {j, 0}, {j + 0.2, 0.4}}]
    }
  ]
];
Draw[GD[Knot[8, 17]]]
```



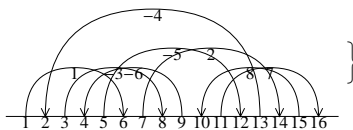
```

βSimplify = Factor;
SetAttributes[βCollect, Listable];
βCollect[B[ω_, μ_]] := B[
  βSimplify[ω],
  Collect[μ, _h, Collect[#, _t, βSimplify] &]
];
(* "L" for "Labels" *)
hL[β_] := Union[Cases[β, h[s_] => s, Infinity]];
tL[β_] := Union[Cases[β, t[s_] | T_s_ => s, Infinity]];
dL[β_] := Union[hL[β], tL[β]];
SetAttributes[βForm, Listable];
βForm[B[ω_, μ_]] := Module[
  {tails, heads, mat},
  tails = tL[B[ω, μ]]; heads = hL[B[ω, μ]];
  mat = Outer[βSimplify[Coefficient[μ, h[#1] t[#2]]] &, heads, tails];
  PrependTo[mat, t /@ tails];
  mat = Prepend[Transpose[mat], Prepend[h /@ heads, ω]];
  MatrixForm[mat]
];

R[x_, y_] := B[1, (T_x - 1) t[x] h[y]];
Rinv[x_, y_] := B[1, (1 / T_x - 1) t[x] h[y]];
tm[x_, y_, z_][β_] := β /. {t[x] -> t[z], t[y] -> t[z], T_x -> T_z, T_y -> T_z};
hm[x_, y_, z_][B[ω_, μ_]] := Module[
  {γx = D[μ, h[x]], γy = D[μ, h[y]], M = μ /. h[x] | h[y] -> 0},
  B[ω, M + h[z] (γx + γy + (γx /. t[i_] -> 1) γy)] // βCollect
];
swap[x_, y_][B[ω_, μ_]] := Module[
  {α, β, γ, δ, ε},
  α = Coefficient[μ, h[x] t[y]];
  β = D[μ, t[y]] /. h[x] -> 0;
  γ = D[μ, h[x]] /. t[y] -> 0;
  δ = μ /. h[x] | t[y] -> 0;
  ε = 1 + α;
  B[ω * ε, Plus[
    α (1 + (γ /. t[i_] -> 1) / ε) h[x] t[y],
    β (1 + (γ /. t[i_] -> 1) / ε) t[y],
    γ / ε h[x],
    δ - (1 / ε) γ * β
  ]] // βCollect
];
gm[x_, y_, z_][β_] := β // swap[y, x] // hm[x, y, z] // tm[x, y, z];
B /: B[ω1_, μ1_] B[ω2_, μ2_] := B[ω1 * ω2, μ1 + μ2];

```

```
{Alexander[K = Knot[8, 17]][X], Draw[GD[K]]}
```

$$\left\{ 11 - \frac{1}{X^3} + \frac{4}{X^2} - \frac{8}{X} - 8X + 4X^2 - X^3, \right.$$


```
(β = Times @@ GD[K] /. {Ar[x_, y_, +1] => R[x, y], Ar[x_, y_, -1] => Rinv[x, y]}) // βForm
```

	1	h[2]	h[4]	h[6]	h[8]	h[10]	h[12]	h[14]	h[16]
t[1]	0	0	-1 + T ₁	0	0	0	0	0	0
t[3]	0	0	0	$-\frac{-1+T_3}{T_3}$	0	0	0	0	0
t[5]	0	0	0	0	0	$-\frac{-1+T_5}{T_5}$	0	0	0
t[7]	0	0	0	0	0	0	-1 + T ₇	0	0
t[9]	0	$-\frac{-1+T_9}{T_9}$	0	0	0	0	0	0	0
t[11]	0	0	0	0	0	0	0	-1 + T ₁₁	0
t[13]	$-\frac{-1+T_{13}}{T_{13}}$	0	0	0	0	0	0	0	0
t[15]	0	0	0	0	-1 + T ₁₅	0	0	0	0

```
Flatten[{
  βForm[β =
    Times @@ GD[K] /. {Ar[x_, y_, +1] => R[x, y], Ar[x_, y_, -1] => Rinv[x, y]},
  Table[
    {k,
      (β = β // gm[1, k, 1]) // βForm,
      Collect[Last[β] /. t[i_] => 1, _h, FullSimplify],
      Collect[Last[β] /. h[i_] => 1, _t, FullSimplify]
    },
    {k, 2, 2 Crossings[K]}
  ]
}] // ColumnForm
```

	1	h[2]	h[4]	h[6]	h[8]	h[10]	h[12]	h[14]	h[16]
t[1]	0	0	-1 + T ₁	0	0	0	0	0	0
t[3]	0	0	0	$-\frac{-1+T_3}{T_3}$	0	0	0	0	0
t[5]	0	0	0	0	0	$-\frac{-1+T_5}{T_5}$	0	0	0
t[7]	0	0	0	0	0	0	-1 + T ₇	0	0
t[9]	0	$-\frac{-1+T_9}{T_9}$	0	0	0	0	0	0	0
t[11]	0	0	0	0	0	0	0	-1 + T ₁₁	0
t[13]	$-\frac{-1+T_{13}}{T_{13}}$	0	0	0	0	0	0	0	0
t[15]	0	0	0	0	-1 + T ₁₅	0	0	0	0

$$\begin{pmatrix} 1 & h[1] & h[4] & h[6] & h[8] & h[10] & h[12] & h[14] & h[16] \\ t[1] & 0 & 0 & \frac{-1+T_1}{T_{13}} & 0 & 0 & 0 & 0 & 0 \\ t[3] & 0 & 0 & 0 & -\frac{-1+T_3}{T_3} & 0 & 0 & 0 & 0 \\ t[5] & 0 & 0 & 0 & 0 & 0 & -\frac{-1+T_5}{T_5} & 0 & 0 \\ t[7] & 0 & 0 & 0 & 0 & 0 & 0 & -1+T_7 & 0 \\ t[9] & 0 & -\frac{-1+T_9}{T_9} & 0 & 0 & 0 & 0 & 0 & 0 \\ t[11] & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1+T_{11} \\ t[13] & -\frac{-1+T_{13}}{T_{13}} & 0 & \frac{(-1+T_1)(-1+T_{13})}{T_{13}} & 0 & 0 & 0 & 0 & 0 \\ t[15] & 0 & 0 & 0 & 0 & -1+T_{15} & 0 & 0 & 0 \end{pmatrix}$$

$$h[6] \left(-1 + \frac{1}{T_1}\right) + h[8] \left(-1 + \frac{1}{T_3}\right) + h[12] \left(-1 + \frac{1}{T_5}\right) + h[14] (-1 + T_7) + h[4] \left(-1 + \frac{1}{T_9}\right) + h[16] (-1 + T_{11}) + \frac{(-1+T_1)t[1]}{T_{13}} + \left(-1 + \frac{1}{T_3}\right) t[3] + \left(-1 + \frac{1}{T_5}\right) t[5] + (-1 + T_7) t[7] + \left(-1 + \frac{1}{T_9}\right) t[9] + (-1 + T_{11}) t[11] + \frac{(-1+T_{13})t[13]}{T_{13}} + (-1 + T_{15}) t[15]$$

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$$\begin{pmatrix} 1 & h[1] & h[4] & h[6] & h[8] & h[10] & h[12] & h[14] & h[16] \\ t[1] & 0 & 0 & \frac{-1+T_1}{T_{13}} & -\frac{-1+T_1}{T_1} & 0 & 0 & 0 & 0 \\ t[5] & 0 & 0 & 0 & 0 & 0 & -\frac{-1+T_5}{T_5} & 0 & 0 \\ t[7] & 0 & 0 & 0 & 0 & 0 & 0 & -1+T_7 & 0 \\ t[9] & 0 & -\frac{-1+T_9}{T_9} & 0 & 0 & 0 & 0 & 0 & 0 \\ t[11] & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1+T_{11} \\ t[13] & -\frac{-1+T_{13}}{T_{13}} & 0 & \frac{(-1+T_1)(-1+T_{13})}{T_{13}} & 0 & 0 & 0 & 0 & 0 \\ t[15] & 0 & 0 & 0 & 0 & -1+T_{15} & 0 & 0 & 0 \end{pmatrix}$$

$$h[8] \left(-1 + \frac{1}{T_1}\right) + h[6] (-1 + T_1) + h[12] \left(-1 + \frac{1}{T_5}\right) + h[14] (-1 + T_7) + h[4] \left(-1 + \frac{1}{T_9}\right) + h[16] (-1 + T_{11}) + \left(-1 + \frac{1}{T_1} + \frac{-1+T_1}{T_{13}}\right) t[1] + \left(-1 + \frac{1}{T_5}\right) t[5] + (-1 + T_7) t[7] + \left(-1 + \frac{1}{T_9}\right) t[9] + (-1 + T_{11}) t[11] + \frac{(-2+T_1)(-1+T_{13})t[13]}{T_{13}} + (-1 + T_{15}) t[15]$$

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$$\begin{pmatrix} 1 & h[1] & h[6] & h[8] & h[10] & h[12] & h[14] & h[16] \\ t[1] & 0 & \frac{-1+T_1}{T_9 T_{13}} & -\frac{-1+T_1}{T_1 T_9} & 0 & 0 & 0 & 0 \\ t[5] & 0 & 0 & 0 & 0 & -\frac{-1+T_5}{T_5} & 0 & 0 \\ t[7] & 0 & 0 & 0 & 0 & 0 & -1+T_7 & 0 \\ t[9] & -\frac{-1+T_9}{T_9 T_{13}} & \frac{(-1+T_1)(-1+T_9)}{T_9 T_{13}} & -\frac{(-1+T_1)(-1+T_9)}{T_1 T_9} & 0 & 0 & 0 & 0 \\ t[11] & 0 & 0 & 0 & 0 & 0 & 0 & -1+T_{11} \\ t[13] & -\frac{-1+T_{13}}{T_{13}} & \frac{(-1+T_1)(-1+T_{13})}{T_{13}} & 0 & 0 & 0 & 0 & 0 \\ t[15] & 0 & 0 & 0 & -1+T_{15} & 0 & 0 & 0 \end{pmatrix}$$

$$h[8] \left(-1 + \frac{1}{T_1}\right) + h[6] (-1 + T_1) + h[12] \left(-1 + \frac{1}{T_5}\right) + h[14] (-1 + T_7) + h[16] (-1 + T_{11}) + h[1] \left(-1 + \frac{1}{T_9}\right) + \frac{(-1+T_1)(T_1-T_{13})t[1]}{T_9 T_9 T_{13}} + \left(-1 + \frac{1}{T_5}\right) t[5] + (-1 + T_7) t[7] + \frac{(-1+T_9)(T_1^2+T_{13}-T_1(2+T_{13}))t[9]}{T_1 T_9 T_{13}} + (-1 + T_{11}) t[11] + \frac{(-1+T_{13})t[13]}{T_{13}} + (-1 + T_{15}) t[15]$$

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$$\begin{pmatrix} 1 & h[1] & h[6] & h[8] & h[10] & h[12] & h[14] & h[16] \\ t[1] & 0 & \frac{-1+T_1}{T_9 T_{13}} & -\frac{-1+T_1}{T_1 T_9} & 0 & -\frac{-1+T_1}{T_1} & 0 & 0 \\ t[7] & 0 & 0 & 0 & 0 & 0 & -1 + T_7 & 0 \\ t[9] & -\frac{-1+T_9}{T_9 T_{13}} & \frac{(-1+T_1)(-1+T_9)}{T_9 T_{13}} & -\frac{(-1+T_1)(-1+T_9)}{T_1 T_9} & 0 & 0 & 0 & 0 \\ t[11] & 0 & 0 & 0 & 0 & 0 & 0 & -1 + T_{11} \\ t[13] & -\frac{-1+T_{13}}{T_{13}} & \frac{(-1+T_1)(-1+T_{13})}{T_{13}} & 0 & 0 & 0 & 0 & 0 \\ t[15] & 0 & 0 & 0 & -1 + T_{15} & 0 & 0 & 0 \end{pmatrix}$$

$$h[8] \left(-1 + \frac{1}{T_1}\right) + h[12] \left(-1 + \frac{1}{T_1}\right) + h[6] (-1 + T_1) + h[14] (-1 + T_7) + h[16] (-1 + T_{11}) + h[1] \left(-1 + \frac{(-1+T_1)(T_1-(1+T_9)T_{13})t[1]}{T_1 T_9 T_{13}} + (-1 + T_7) t[7] + \frac{(-1+T_9)(T_1^2+T_{13}-T_1(2+T_{13}))t[9]}{T_1 T_9 T_{13}} + (-1 + T_{11}) t[11] + \frac{(-2+T_1)(-1+T_{13})t[13]}{T_{13}}\right)$$

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$$\begin{pmatrix} \frac{-1+T_1+T_9 T_{13}}{T_9 T_{13}} & h[1] & h[8] & h[10] & h[12] & h[14] & h[16] \\ t[1] & \frac{(-1+T_1) T_1}{T_9 T_{13} (-1+T_1+T_9 T_{13})} & -\frac{(-1+T_1) T_{13}}{-1+T_1+T_9 T_{13}} & 0 & -\frac{(-1+T_1) T_9 T_{13}}{-1+T_1+T_9 T_{13}} & 0 & 0 \\ t[7] & 0 & 0 & 0 & 0 & -1 + T_7 & 0 \\ t[9] & -\frac{-1+T_9}{-1+T_1+T_9 T_{13}} & -\frac{(-1+T_1)(-1+T_9) T_{13}}{T_1 (-1+T_1+T_9 T_{13})} & 0 & \frac{(-1+T_1)^2 (-1+T_9)}{T_1 (-1+T_1+T_9 T_{13})} & 0 & 0 \\ t[11] & 0 & 0 & 0 & 0 & 0 & -1 + T_{11} \\ t[13] & -\frac{T_9 (-1+T_{13})}{-1+T_1+T_9 T_{13}} & \frac{(-1+T_1)^2 (-1+T_{13})}{T_1 (-1+T_1+T_9 T_{13})} & 0 & \frac{(-1+T_1)^2 T_9 (-1+T_{13})}{T_1 (-1+T_1+T_9 T_{13})} & 0 & 0 \\ t[15] & 0 & 0 & -1 + T_{15} & 0 & 0 & 0 \end{pmatrix}$$

$$h[8] \left(-1 + \frac{1}{T_1}\right) + h[12] \left(-1 + \frac{1}{T_1}\right) + h[14] (-1 + T_7) + h[16] (-1 + T_{11}) + h[1] \left(-1 + \frac{T_1}{T_9 T_{13}}\right) + h[10] \left(-\frac{(-1+T_1)(T_1-T_9(1+T_9)T_{13}^2)t[1]}{T_9 T_{13} (-1+T_1+T_9 T_{13})} + (-1 + T_7) t[7] + \frac{(-1+T_9)(1+T_1^2+T_{13}-T_1(3+T_{13}))t[9]}{T_1 (-1+T_1+T_9 T_{13})} + (-1 + T_{11}) t[11] + \frac{((-1+T_1)^2 + (-1+T_9)T_{13})t[13]}{T_1 (-1+T_1+T_9 T_{13})}\right)$$

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$$\begin{pmatrix} \frac{-1+T_1+T_9 T_{13}}{T_9 T_{13}} & h[1] & h[8] & h[10] & h[12] & h[14] & h[16] \\ t[1] & \frac{(-1+T_1) T_1}{T_9 T_{13} (-1+T_1+T_9 T_{13})} & -\frac{(-1+T_1) T_{13}}{-1+T_1+T_9 T_{13}} & 0 & -\frac{(-1+T_1) T_9 T_{13}}{-1+T_1+T_9 T_{13}} & -1 + T_1 & 0 \\ t[9] & -\frac{-1+T_9}{-1+T_1+T_9 T_{13}} & -\frac{(-1+T_1)(-1+T_9) T_{13}}{T_1 (-1+T_1+T_9 T_{13})} & 0 & \frac{(-1+T_1)^2 (-1+T_9)}{T_1 (-1+T_1+T_9 T_{13})} & 0 & 0 \\ t[11] & 0 & 0 & 0 & 0 & 0 & -1 + T_{11} \\ t[13] & -\frac{T_9 (-1+T_{13})}{-1+T_1+T_9 T_{13}} & \frac{(-1+T_1)^2 (-1+T_{13})}{T_1 (-1+T_1+T_9 T_{13})} & 0 & \frac{(-1+T_1)^2 T_9 (-1+T_{13})}{T_1 (-1+T_1+T_9 T_{13})} & 0 & 0 \\ t[15] & 0 & 0 & -1 + T_{15} & 0 & 0 & 0 \end{pmatrix}$$

$$h[8] \left(-1 + \frac{1}{T_1}\right) + h[12] \left(-1 + \frac{1}{T_1}\right) + h[14] (-1 + T_1) + h[16] (-1 + T_{11}) + h[1] \left(-1 + \frac{T_1}{T_9 T_{13}}\right) + h[10] \left(-\frac{(-1+T_1)(T_1+(-1+T_1)T_9 T_{13}-T_9 T_{13}^2)t[1]}{T_9 T_{13} (-1+T_1+T_9 T_{13})} + \frac{(-1+T_9)(1+T_1^2+T_{13}-T_1(3+T_{13}))t[9]}{T_1 (-1+T_1+T_9 T_{13})} + (-1 + T_{11}) t[11] + \frac{((-1+T_1)^2 + (1+(-3+T_1)T_1)T_9 T_{13})t[13]}{T_1 (-1+T_1+T_9 T_{13})}\right)$$

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$$\begin{pmatrix} \frac{-1+T_1+T_{13}-T_1 T_{13}+T_9 T_{13}}{T_9 T_{13}} & h[1] & h[10] & h[12] & h[14] \\ t[1] & \frac{(-1+T_1)(-1+T_{13})}{T_9 T_{13} (1-T_1-T_{13}+T_1 T_{13}-T_9 T_{13})} & 0 & \frac{(-1+T_1) T_9 T_{13}}{T_1 (1-T_1-T_{13}+T_1 T_{13}-T_9 T_{13})} & -\frac{(-1+T_1)(-1+T_1+T_9 T_{13})}{T_1 (1-T_1-T_{13}+T_1 T_{13}-T_9 T_{13})} \\ t[9] & -\frac{-1+T_9}{-1+T_1+T_{13}-T_1 T_{13}+T_9 T_{13}} & 0 & \frac{(-1+T_1)^2 (-1+T_9)(-1+T_{13})}{T_1 (1-T_1-T_{13}+T_1 T_{13}-T_9 T_{13})} & -\frac{(-1+T_1)^2 (-1+T_9) T_{13}}{T_1 (1-T_1-T_{13}+T_1 T_{13}-T_9 T_{13})} \\ t[11] & 0 & 0 & 0 & 0 \\ t[13] & -\frac{(-1+T_1-T_9)(-1+T_{13})}{1-T_1-T_{13}+T_1 T_{13}-T_9 T_{13}} & 0 & -\frac{(-1+T_1)^2 T_9 (-1+T_{13})}{T_1 (1-T_1-T_{13}+T_1 T_{13}-T_9 T_{13})} & \frac{(-1+T_1)^3 (-1+T_{13})}{T_1 (1-T_1-T_{13}+T_1 T_{13}-T_9 T_{13})} \\ t[15] & 0 & -1 + T_{15} & 0 & 0 \end{pmatrix}$$

$$h[12] \left(-1 + \frac{1}{T_1}\right) + h[14] (-1 + T_1) + h[16] (-1 + T_{11}) + h[1] \left(-1 + \frac{1}{T_9 T_{13}}\right) + h[10] (-1 + T_{15}) - \frac{(-1+T_1)(T_1+(T_1(-1+T_9)-T_9)T_{13})t[1]}{T_1 T_9 T_{13} (1+T_1(-1+T_{13})-(1+T_9)T_{13})} - \frac{(1+(-3+T_1)T_1)(-1+T_9)t[9]}{T_1 (1+T_1(-1+T_{13})-(1+T_9)T_{13})} + (-1 + T_{11}) t[11] + \frac{(1+(-3+T_1)T_1)(-1+T_1-T_9)(-1+T_{13})t[13]}{T_1 (1+T_1(-1+T_{13})-(1+T_9)T_{13})}$$

9

$$\begin{pmatrix} \frac{-1+T_1+T_{13}}{T_1 T_{13}} & h[1] & h[10] & h[12] & h[14] \\ t[1] & -\frac{(-1+T_1)(-1+T_{13}+T_1 T_{13})}{T_1 T_{13}(-1+T_1+T_{13})} & 0 & -\frac{(-1+T_1)(-1+2 T_1-T_1^2+T_{13}-T_1 T_{13}+T_1^2 T_{13})}{T_1(-1+T_1+T_{13})} & \frac{(-1+T_1)(-1+T_1+T_{13}-T_1 T_{13}+T_1^2 T_{13})}{T_1(-1+T_1+T_{13})} \\ t[11] & 0 & 0 & 0 & 0 \\ t[13] & -\frac{-1+T_{13}}{-1+T_1+T_{13}} & 0 & \frac{(-1+T_1)^2(-1+T_{13})}{-1+T_1+T_{13}} & -\frac{(-1+T_1)^3(-1+T_{13})}{T_1(-1+T_1+T_{13})} \\ t[15] & 0 & -1+T_{15} & 0 & 0 \end{pmatrix}$$

$$h[12] \left(-1 + \frac{1}{T_1}\right) + h[14] (-1 + T_1) + h[16] (-1 + T_{11}) + h[1] \left(-1 + \frac{1}{T_1 T_{13}}\right) + h[10] (-1 + T_{15})$$

$$\left(\frac{1}{T_1 T_{13}} + \frac{1+(-3+T_1) T_1}{-1+T_1+T_{13}}\right) t[1] + (-1 + T_{11}) t[11] + \frac{(1+(-3+T_1) T_1)(-1+T_{13}) t[13]}{T_1(-1+T_1+T_{13})} + (-1 + T_{15}) t[15]$$

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$$\begin{pmatrix} \frac{-1+T_1+T_{13}}{T_1 T_{13}} & h[1] & h[12] & h[14] \\ t[1] & -\frac{(-1+T_1)(-1+T_{13}+T_1 T_{13}) T_{15}}{T_1 T_{13}(-1+T_1+T_{13})} & -\frac{(-1+T_1)(-1+2 T_1-T_1^2+T_{13}-T_1 T_{13}+T_1^2 T_{13}) T_{15}}{T_1(-1+T_1+T_{13})} & \frac{(-1+T_1)(-1+T_1+T_{13}-T_1 T_{13}+T_1^2 T_{13}) T_{15}}{T_1(-1+T_1+T_{13})} \\ t[11] & 0 & 0 & 0 \\ t[13] & -\frac{-1+T_{13}}{-1+T_1+T_{13}} & \frac{(-1+T_1)^2(-1+T_{13})}{-1+T_1+T_{13}} & -\frac{(-1+T_1)^3(-1+T_{13})}{T_1(-1+T_1+T_{13})} \\ t[15] & \frac{T_1(-1+T_{15})}{-1+T_1+T_{13}} & \frac{(-1+T_1)(-1+2 T_1-T_1^2+T_{13}-T_1 T_{13}+T_1^2 T_{13})(-1+T_{15})}{T_1(-1+T_1+T_{13})} & -\frac{(-1+T_1)(-1+T_1+T_{13}-T_1 T_{13}+T_1^2 T_{13})(-1+T_{15})}{T_1(-1+T_1+T_{13})} \end{pmatrix}$$

$$h[12] \left(-1 + \frac{1}{T_1}\right) + h[14] (-1 + T_1) + h[16] (-1 + T_{11}) + h[1] \left(-1 + \frac{T_{15}}{T_1 T_{13}}\right)$$

$$\frac{(-1+T_1)(1+(-1+(-2+T_1) T_1) T_{13}) T_{15} t[1]}{T_1 T_{13}(-1+T_1+T_{13})} + (-1 + T_{11}) t[11] + \frac{(1+(-3+T_1) T_1)(-1+T_{13}) t[13]}{T_1(-1+T_1+T_{13})} - \frac{(1+(-3+T_1) T_1)(-1+T_{15}) t[15]}{-1+T_1+T_{13}}$$

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$$\begin{pmatrix} \frac{-1+T_1+T_{13}}{T_1 T_{13}} & h[1] & h[12] & h[14] \\ t[1] & -\frac{(-1+T_1)(-1+T_{13}+T_1 T_{13}) T_{15}}{T_1 T_{13}(-1+T_1+T_{13})} & -\frac{(-1+T_1)(-1+2 T_1-T_1^2+T_{13}-T_1 T_{13}+T_1^2 T_{13}) T_{15}}{T_1(-1+T_1+T_{13})} & \frac{(-1+T_1)(-1+T_1+T_{13}-T_1 T_{13}+T_1^2 T_{13}) T_{15}}{T_1(-1+T_1+T_{13})} \\ t[13] & -\frac{-1+T_{13}}{-1+T_1+T_{13}} & \frac{(-1+T_1)^2(-1+T_{13})}{-1+T_1+T_{13}} & -\frac{(-1+T_1)^3(-1+T_{13})}{T_1(-1+T_1+T_{13})} \\ t[15] & \frac{T_1(-1+T_{15})}{-1+T_1+T_{13}} & \frac{(-1+T_1)(-1+2 T_1-T_1^2+T_{13}-T_1 T_{13}+T_1^2 T_{13})(-1+T_{15})}{T_1(-1+T_1+T_{13})} & -\frac{(-1+T_1)(-1+T_1+T_{13}-T_1 T_{13}+T_1^2 T_{13})(-1+T_{15})}{T_1(-1+T_1+T_{13})} \end{pmatrix}$$

$$h[12] \left(-1 + \frac{1}{T_1}\right) + h[14] (-1 + T_1) + h[16] (-1 + T_1) + h[1] \left(-1 + \frac{T_{15}}{T_1 T_{13}}\right)$$

$$\left(-1 + T_1 + \frac{(-1+T_1)(1+(-1+(-2+T_1) T_1) T_{13}) T_{15}}{T_1 T_{13}(-1+T_1+T_{13})}\right) t[1] + \frac{(1+(-3+T_1) T_1)(-1+T_{13}) t[13]}{T_1(-1+T_1+T_{13})} - \frac{(1+(-3+T_1) T_1)(-1+T_{15}) t[15]}{-1+T_1+T_{13}}$$

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$$\begin{pmatrix} -\frac{T_1-T_1^2-T_1 T_{13}+T_{15}-3 T_1 T_{15}+3 T_1^2 T_{15}-T_1^3 T_{15}-T_{13} T_{15}+2 T_1 T_{13} T_{15}-2 T_1^2 T_{13} T_{15}+T_1^3 T_{13} T_{15}}{T_1^2 T_{13}} & h[1] \\ t[1] & \frac{(-1+T_1) T_{15}(-T_1+T_1 T_{13}+T_1^2 T_{13}-T_{15}+2 T_1 T_{15}-T_1 T_1^2 T_{13}-T_1 T_{13}+T_{15}-3 T_1 T_{15}+3 T_1^2 T_{15}-T_1^3 T_{15}-T_1)}{T_1^2 T_{13} (T_1-T_1^2-T_1 T_{13}+T_{15}-3 T_1 T_{15}+3 T_1^2 T_{15}-T_1^3 T_{15}-T_1)} \\ t[13] & -\frac{(-1+T_{13})(-T_1-T_{15}+2 T_1 T_1)}{T_1-T_1^2-T_1 T_{13}+T_{15}-3 T_1 T_{15}+3 T_1^2 T_{15}-T_1^3 T_{15}-T_{13} T_{15}} \\ t[15] & -\frac{T_1^2(-1+T_{15})}{T_1-T_1^2-T_1 T_{13}+T_{15}-3 T_1 T_{15}+3 T_1^2 T_{15}-T_1^3 T_{15}-T_{13} T_{15}} \end{pmatrix}$$

$$h[14] (-1 + T_1) + h[16] (-1 + T_1) + h[1] \left(-1 + \frac{T_{15}}{T_1^2 T_{13}}\right)$$

$$\frac{(-1+T_1)(-T_1^2 T_{13}(-1+T_1+T_{13})-T_1(1+T_{13}(-2+(1+(-1+T_1) T_1) T_{13}))) T_{15} + (-1+T_1)^2 + (1+(-1+T_1) T_1) T_{13} T_{15}^2}{T_1^2 T_{13} (-T_1(-1+T_1+T_{13}) + (-1+T_1)(-1+T_1)^2 + (1+(-1+T_1) T_1) T_{13} T_{15})} t[1] + \frac{(-1+T_{13})(T_1(-1+3 T_1-T_1^2))}{T_1(-T_1(-1+T_1+T_{13}) + (-1+T_1)(-1+T_1)^2 + (1+(-1+T_1) T_1) T_{13} T_{15})}$$

13

$$\begin{pmatrix} -\frac{T_1-2 T_1^2+T_{15}-4 T_1 T_{15}+5 T_1^2 T_{15}-3 T_1^3 T_{15}+T_1^4 T_{15}}{T_1^4} & h[1] \\ t[1] & -\frac{(-1+T_1)(-T_1^4+T_1 T_{15}-T_1^2 T_{15}-2 T_1^3 T_{15}+2 T_1^4 T_{15}-2 T_1^5 T_{15}+T_1^6 T_{15}+T_1^7 T_{15}+T_{15}^2-3 T_1 T_{15}^2+2 T_1^2 T_{15}^2-T_1^3 T_{15}^2)}{T_1^4 (T_1-2 T_1^2+T_{15}-4 T_1 T_{15}+5 T_1^2 T_{15}-3 T_1^3 T_{15}+T_1^4 T_{15})} \\ t[15] & -\frac{T_1^2(-1+T_{15})}{T_1-2 T_1^2+T_{15}-4 T_1 T_{15}+5 T_1^2 T_{15}-3 T_1^3 T_{15}+T_1^4 T_{15}} \end{pmatrix}$$

$$h[14] (-1 + T_1) + h[16] (-1 + T_1) + h[1] \left(-1 + \frac{T_{15}}{T_1^2}\right)$$

$$\frac{(-1+T_1) (T_1^4-2 T_1^5+T_1^7+(-1+T_1) T_1 (1+T_1^2 (-4+(-2+T_1)^2 T_1))) T_{15}+(-1+T_1 (3+(-2+T_1) T_1)) T_{15}^2}{T_1^3 (T_{15}+T_1 (1-2 T_1+(-4+T_1 (5+(-3+T_1) T_1)) T_{15}))} t[1] + \frac{T_1 (2+T_1 (-7+T_1 (6+(-3+T_1) T_1))) (-1+T_1)}{T_{15}+T_1 (1-2 T_1+(-4+T_1 (5+(-3+T_1) T_1)) T_1)}$$

14

$$\left(\begin{array}{c} -\frac{1-3 T_1+4 T_1^2-4 T_1^3+T_1^4-T_{15}+4 T_1 T_{15}-7 T_1^2 T_{15}+7 T_1^3 T_{15}-4 T_1^4 T_{15}+T_1^5 T_{15}}{T_1^3} \\ t[1] \\ t[15] \end{array} \right) \begin{array}{c} h[1] \\ -\frac{(-1+T_1) (-T_1^4+T_{15}-2 T_1 T_{15}+2 T_1^2 T_{15}-3 T_1^3 T_{15}+2 T_1^4 T_{15}-2 T_1^5 T_{15}+T_1^6 T_{15}}{T_1^2 (1-3 T_1+4 T_1^2-4 T_1^3+T_1^4-T_{15}+4 T_1 T_{15}-7 T_1^2 T_{15}+7 T_1^3 T_{15}-4 T_1^4 T_{15}+T_1^5 T_{15})} \\ \frac{(1-3 T_1+3 T_1^2-3 T_1^3+T_1^4) (-1+T_{15})}{1-3 T_1+4 T_1^2-4 T_1^3+T_1^4-T_{15}+4 T_1 T_{15}-7 T_1^2 T_{15}+7 T_1^3 T_{15}-4 T_1^4 T_{15}+T_1^5 T_{15}} \end{array}$$

$$h[16] (-1 + T_1) + h[1] \left(-1 + \frac{T_{15}}{T_1^2}\right)$$

$$\frac{(-1+T_1) ((-1+T_1) T_1^3 (-1+(-1+T_1)^2 T_1) - (1+T_1 (1+(-1+T_1) T_1) (-2+(-1+T_1) T_1^2))) T_{15}+(-1+T_1)^2 (1+(-1+T_1) T_1) T_{15}^2}{T_1^2 (1-3 T_1+4 T_1^2-4 T_1^3+T_1^4+(-1+T_1)^3 (1+(-1+T_1) T_1) T_{15})} t[1] + \frac{(2+(-2+T_1) T_1) (1+T_1)}{1-3 T_1+4 T_1^2}$$

15

$$\left(\begin{array}{cc} -\frac{1-4 T_1+8 T_1^2-11 T_1^3+8 T_1^4-4 T_1^5+T_1^6}{T_1^3} & h[1] \quad h[16] \\ t[1] & -\frac{1+T_1}{T_1} \quad -1 + T_1 \end{array} \right)$$

$$h[1] \left(-1 + \frac{1}{T_1}\right) + h[16] (-1 + T_1)$$

$$\left(-2 + \frac{1}{T_1} + T_1\right) t[1]$$

16

$$\left(\begin{array}{c} -\frac{1-4 T_1+8 T_1^2-11 T_1^3+8 T_1^4-4 T_1^5+T_1^6}{T_1^2} \\ t[1] \end{array} \right)$$

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